# Better 2-round adaptive MPC

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- 2. simulate r<sub>i</sub> of corrupted parties, consistent with communication and x<sub>i</sub>



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Example: encryption





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#### Simulator:

- 1. simulate fake ciphertext c (without knowing m)
- 2. upon corruption, learn m and provide consistent r, sk

Example: encryption



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### Full adaptive security for randomized functionalities:

 Randomness of the computation remains hidden even when all parties are corrupted

Example: F internally chooses random primes p, q, and outputs N = pq. Most protocols (e.g. CLOS02) reveal p, q, when all parties are corrupted.

	# of parties	# of rounds	assumptions
Canetti, Goldwasser, Poburinnaya'15	2	2	OWF subexp iO
Dachman-Soled, Katz, Rao'15	n	4	OWF iO
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Only 3 fully adaptively secure protocols with constant rounds - but with a CRS\* Only one of them is 2 round MPC.

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This work	n	2	injective OWF iO	+	+ (comp. close)

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### Part I:

**Theorem** (informal):

Assuming indistinguishability obfuscation for circuits and injective one way functions,

there exists 2-round, fully-adaptively-secure, RAM-efficient semi-honest MPC protocol where:

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#### Part II:

**Theorem** (informal): Assuming iO for circuits and TDPs, there exists **RAM-efficient statistically sound NIZK**.

**Theorem** (GP15, our work): Assuming subexp. iO for circuits and RAM-efficient statistically sound NIZK, there exists **2-round, fully-adaptively-secure, RAM-efficient byzantine** MPC protocol.

### Part I: HBC protocol with global CRS

### First attempt

$$\mathbf{x}_{i}$$
 = Enc<sub>PK</sub>( $\mathbf{x}_{i}$ )



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## Our protocol

- $\mathbf{x}_{i}$  = Commit( $\mathbf{x}_{i}$ ;  $\mathbf{r}_{i}$ )
- $|\mathbf{x}_{i}|^{r_{i}} = \operatorname{Enc}_{\mathsf{PK}}(\mathbf{x}_{i}||\mathbf{r}_{i}|| \square \square ... \square )$








# Required primitives







honestly generated is statistically binding.















\*: Simulation-secure analog of Sahai-Waters PDE

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Solution: Modify the protocol to choose PK, SK during the execution.



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Ishai-Kushilevitz paradigm: use MPC to evaluate garbling:  $F(x_1, ..., x_n; r) = garbled f, garbled x_1, ..., x_n$ .







### How to make the protocol RAM-efficient: two ways



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(requires subexp. iO)

### Part II: Byzantine protocol and NIZK for RAM

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GP'15 doesn't compute randomness-hiding functionalities, i.e.IK02 approach doesn't work.

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Observation: GP'15 works with circuits only because of NIZK proof of the statement  $f(x_1, ..., x_n) = y$ . In all NIZK proofs so far: the work of verifier ~ circuit size of f.

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**Theorem** (Garg-Polychroniadou'15): Assuming iO for RAM, one way functions, and **NIZK proofs for RAM**, there exists **2-round, fully-adaptively-secure, RAM-efficient** MPC protocol against **malicious adversaries**.

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Theorem (Our work): Assuming garbling scheme for RAM and NIZK proofs for circuits, there exists **statistically sound NIZK proof system** for RAM.

NIZK proof system:

Let language L be defined by relation R(x; w) Prove(x, w)  $\rightarrow \pi$ Verify(x,  $\pi$ )  $\rightarrow$  accept / reject

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Completeness; Statistical soundness; Zero-knowledge; RAM-efficient\*:

- work of P only depends on |R|<sub>RAM</sub>
- $|\pi|$  only depends on  $|\mathsf{R}|_{\mathsf{RAM}}$
- work of V depends on RÄM complexity of R

\*: everything also depends on |x|, |w|.

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Garbling scheme:KeyGen(r)  $\rightarrow$  kGarbleProg(k, f)  $\rightarrow$  fGarbleInput(k, x)  $\rightarrow$  x

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**Correctness:** can compute f(x) **Security**: garbled values only reveal f(x) **RAM-efficient**\*:

- work of the garbler only depends on |f|<sub>RAM</sub>
- size of garbled values depends on |f|<sub>RAM</sub>
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Exists under iO for circuits + OWFs (Canetti-Holmgren'16)

Attempt 1

Convince that  $\exists w$  such that R(x; w) = 1



Prover

 $\mathbf{x} \in \mathbf{L}$ w



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Accept if Eval(

R(\*,\*)

) = 1

X, W











#### • Verifier doesn't learn anything about w


KeyGen(r)  $\rightarrow$  k

GarbleProg(k, R)  $\rightarrow$ 







) = 1

X, W

R(\*,\*)















## Summary: two round adaptively secure protocols

Semi-honest case:

- global CRS
- RAM-efficient
- computes randomized functionalities
- from iO and injective OWFs (no subexp iO)

#### Malicious case (GP15 + our RAM efficient NIZK):

- RAM-efficient
- from subexp iO and TDP

#### **Open questions**

Fully adaptive constant round HBC protocol **without a CRS?** Fully adaptive constant round malicious protocol **without subexp iO?** 

# Questions?